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Dynamic Programming for Routing and Scheduling

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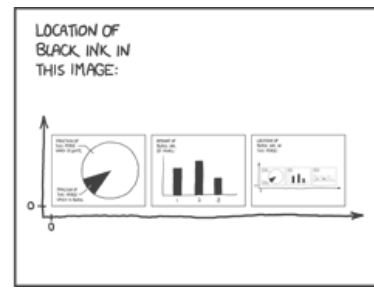
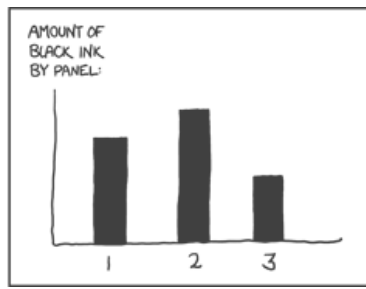
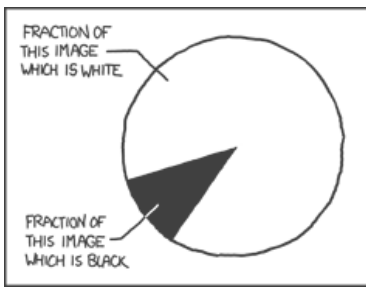
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Contents

Introduction	1
1 Dynamic Programming	5
1.1 The basics of Dynamic Programming	5
1.1.1 Fibonacci numbers	6
1.1.2 Longest common subsequence	8
1.1.3 Knapsack	10
1.1.4 Minimizing redundancy	12
1.2 Dynamic Programming over sets	17
1.2.1 Linear assignment problem	17
1.2.2 Steiner tree in graphs	20
1.2.3 Single machine total weighted tardiness problem	23
2 Sequencing, Routing and Scheduling	27
2.1 Traveling Salesman Problem	28
2.2 Vehicle Routing Problem	29
2.3 Job Shop Scheduling Problem	33
<i>Intermezzo: Antichains</i>	48
3 The Dynamic Programming State Space	51
3.1 Dynamic bounding	51
3.2 Finding all optimal solutions with DP	53
3.3 Heuristic DP algorithms	59
3.3.1 Removing state variables	59
3.3.2 Limiting the number of expansions	60
3.3.3 Limiting the number of solutions to expand	61
3.3.4 Heuristic bounding	62
4 The Vehicle Routing Problem	67
4.1 Dynamic bounding for the VRP	67
4.2 Properties of the Vehicle Routing Problem	69
4.2.1 Precedence relations	69
4.2.2 Symmetric distance matrix	72
4.2.3 Symmetry in the GTR	72

4.3	Variants of the Vehicle Routing Problem	73
4.3.1	Heterogeneous vehicles	73
4.3.2	Capacitated VRP	74
4.3.3	Multiple compartment VRP	75
4.3.4	Pickup and delivery	76
4.3.5	Redistribution	77
4.3.6	Time-windows	78
4.3.7	Driving and working hours regulations	78
4.3.8	Inter-route time constraints	79
4.3.9	Mixing variants	81
4.4	Using DP as pricing instrument	81
5	The Job Shop Scheduling Problem	83
5.1	Dynamic bounding for the JSSP	83
5.1.1	Parallel head–tail adjustments	84
5.2	Finding JSSP solutions	85
5.2.1	No bound	86
5.2.2	Optimal bound	87
5.2.3	Finding solutions	89
5.2.4	Finding lower bounds	89
5.3	All solutions for the JSSP	91
5.3.1	Finding all optimal solutions	93
6	The Job Shop Scheduling Problem with Scheduled Maintenances	97
6.1	Adding maintenances	97
6.2	A Mixed-Integer Programming formulation	98
6.3	Dynamic Programming	101
6.4	Bounding for the JSSPM	104
	<i>Intermezzo: A lower bound for the one-dimensional bin</i>	
	<i>packing problem.</i>	104
6.4.1	Updating heads and tails on a single machine	108
6.4.2	Updating heads and tails on all machines	109
6.4.3	Dynamic bounding for the JSSPM	115
6.5	JSSPM instances	116
6.6	Comparing DP to MIP	118
	Concluding Remarks	121
	Appendix A Computational Results	125
	Vehicle Routing Problem	126
	Job Shop Scheduling Problem	130
	JSSP with scheduled Maintenances	142

Appendix B Job Shop Scheduling Problem Instances	159
Fisher and Thompson	160
Lawrence	160
Adams, Balas, and Zawack	162
Applegate and Cook	162
Storer, Wu, and Vaccari	163
Yamada and Nakano	164
Taillard	164
Demirkol, Mehta, and Uzsoy	167
Glossary of Notation	171
Acronyms	171
Common symbols	171
Dynamic Programming specific symbols	171
Traveling Salesman Problem symbols	172
Vehicle Routing Problem symbols	172
Job Shop Scheduling Problem symbols	172
JSSP with scheduled Maintenances symbols	173
JSSP bounding symbols	173
Bibliography	175
Summary	187
Acknowledgements	189
List of Comics	193

