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Rich dynamics in multi-strain models: Non-linear dynamics and deterministic chaos in dengue fever epidemiology

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